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# High-energy mechanical milling of poly(methyl methacrylate), polyisoprene and poly(ethylene-*alt*-propylene)

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### Abstract

High-energy mechanical milling has been performed on poly(methyl methacrylate) (PMMA) at ambient and cryogenic temperatures, as well as on polyisoprene (PI) and poly(ethylene-*alt*-propylene) (PEP) at cryogenic conditions only. Milling conducted at ambient temperature has a substantially greater impact on the molecular characteristics of PMMA than milling at cryogenic temperatures. An increase in the milling time is accompanied by substantial reductions in PMMA molecular weight and, hence, glass transition temperature and impact strength under both sets of experimental conditions. An unexpected trend identified here is that the PMMA molecular weight distribution initially broadens and subsequently narrows with increasing milling time. Solid-state mechanical milling promotes comparable decreases in molecular weight and glass transition temperature in PEP (at a slower rate relative to PMMA), but induces chemical crosslinking in PI, as confirmed by FTIR spectroscopy. Charlesby–Pinner analysis yields not only the degree of PI crosslinking, but also the relative crosslinking and scission rates of PI, during cryogenic milling. © 2000 Elsevier Science Ltd. All rights reserved.

Keywords: Mechanical milling; Mechanical attrition; Glass transition temperature

# 1. Introduction

Without a doubt, the most significant impediment to producing intimately (nanoscale) mixed blends of dissimilar polymeric materials lies in the intrinsic immiscibility of macromolecules [1,2]. In most conventional processes, polymers are blended in a fashion that endows the chains with sufficient mobility for the constituent polymer species to phase-separate, which is often accompanied by severe degradation of thermal, optical and/or mechanical properties. Since most high-throughput blending techniques rely on melt or solution processing, numerous studies continue to explore physical and reactive compatibilization routes as methods which promote (and retain) intimate polymer dispersion during processing [3-6]. An alternative strategy for producing polymer blends, while avoiding the problem of phase separation, relies on solid-state mixing, which generally involves the efficient grinding of two or more

polymer species [2]. Mechanical action can, however, have deleterious effects on polymers in the solid (glassy or crystalline) state by breaking chains and creating free radicals. For this reason, high-dispersion solid-state blending is only now being realized as a viable technology. Recent years have witnessed resurgence in this process through the increased use of mechanical ball milling [7–11] and solid-state extrusion pulverization [12,13] in preparing polymer blends. The objective of the present work is to explore the effects of high-energy mechanical milling on the molecular and physical properties of single homopolymers, since a fundamental understanding of these effects is prerequisite to the use of mechanical alloying as a means of producing novel polymer blends.

Mechanical milling (involving one material) and mechanical alloying (involving two or more materials) generally refer to high-energy ball-milling techniques employed to process materials in the solid state [14]. These non-equilibrium processing routes, responsible for the early successes in oxide dispersion strengthening of metallic superalloys [15], have expedited production of a wide variety of metastable inorganic materials and morphologies (both single component and alloys), and are

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Sample designation	Reported $\bar{M}_{\rm w}$ (kg mol <sup>-1</sup> )	Measured $\bar{M}_{\rm w}$ (kg mol <sup>-1</sup> )	Measured $\bar{M}_n$ (kg mol <sup>-1</sup> )	PDI	
h-PMMA	996	1040	255	4.08	
m-PMMA	120	121	67.1	1.80	
1-PMMA	15	16.6	14.8	1.12	
n-PMMA	100	92.0	73.8	1.25	
PI	60	72.1	68.8	1.05	
PEP <sup>a</sup>	60	67.1	63.4	1.06	

Table 1 Molecular characteristics of the as-received polymers employed in this study

<sup>a</sup> The difference in molecular weight characteristics between PI and PEP is due to their different hydrodynamic volumes.

presently used to form extended solid solutions, novel intermediate phases, alloys from immiscible metals and oxides, metal-ceramic composites and nanocrystalline materials [14,16,17]. Application of high-energy mechanical milling to polymeric materials, however, remains relatively recent, initiated by Shaw and co-workers in the early 1990s [7,8,18,19]. These and subsequent [9–11,20] investigations have focused primarily on milling-induced structural and property changes in semi-crystalline polymers and their blends, but have not elucidated, in systematic fashion, the molecular physico-chemical changes that occur as a result of milling.

Prior works addressing the mechanochemistry of polymers have often sought to identify and explain the stressinduced molecular changes that arise in molten or solvated polymers during the course of mechanical processes such as grinding, extruding and stirring [21-24]. Issues regarding, for instance, changes in molecular weight and molecular weight distribution, as well as free-radical generation and mechanisms, have received considerable attention in this vein. Although induced by different means, the physicochemical changes of macromolecules due to mechanical milling are expected to be similar to those incurred by these related mechanical processes. A complex combination of shearing, extension, fracture and cold-welding of polymer powder particles during milling may induce chain scission or hydrogen abstraction and generate free radicals. While chain scission would be accompanied by a reduction in molecular weight, it is conceivable that free radicals may promote interchain reactions and, hence, chemical crosslinking.

Modification of a single polymer or a polymer blend by high-energy mechanical milling is therefore anticipated to have a profound effect on the properties of polymeric material(s) in a relatively unpredictable manner. In a recent investigation [25] of poly(ethylene terephthalate) (PET) mechanically milled at ambient and cryogenic temperatures, for example, milling is found to promote amorphism in both high- and low-crystallinity PET. Within this metastable state, the PET chains are highly aligned to form an almost nematic mesophase. Upon post-annealing, the chains readily form crystals, thereby demonstrating that milling has a profound impact on molecular alignment and structure development in some thermoplastic polymers. In the present study, we employ molecular weight (*M*), glass transition temperature ( $T_g$ ) and impact strength measurements to probe the time-dependent molecular and property evolution of three homopolymers—poly(methyl methacrylate) (PMMA), polyisoprene (PI) and poly(ethylene-*alt*-propylene) (PEP)—during high-energy mechanical milling in the solid state.

## 2. Experimental

# 2.1. Materials

Three grades of PMMA differing in number- and weightaverage molecular weight ( $\overline{M}_n$  and  $\overline{M}_w$ , respectively) were purchased from Aldrich and used as-received. In addition, another PMMA homopolymer, as well as a PI homopolymer and its hydrogenated PEP analog were custom-synthesized via living anionic polymerization. The molecular weight characteristics of these six materials, as discerned by gel permeation chromatography (GPC), and their designations are listed in Table 1. The PMMA homopolymers were milled at ambient temperature (ambimilled) and liquid nitrogen temperature (cryomilled), whereas the PI and PEP homopolymers were only subjected to cryomilling due to their low  $T_{gs}$ . In all cases, 3 g of polymer were placed in a hardened steel vial (about 60 ml full capacity) with 30 g of steel ball bearings (6.4 and 7.9 mm in diameter), and the vial was sealed under Ar (with <10 ppm of O<sub>2</sub>). For ambimilling experiments, the sealed vial was placed in a standard SPEX 8000 mill and violently agitated at 20 Hz without any coolant (the external vial temperature remained at 30°C). For cryomilling experiments, the vial was placed in a custom-designed nylon sleeve designed to allow peripheral flow of liquid nitrogen and, hence, maintain a constant external vial temperature (at ca. -180°C) during milling. The vial assembly was placed in a modified SPEX 8000 mill (reinforced to handle the extra mass and torque applied during operation) and vigorously shaken. Specimens were milled for intervals up to 10 h, after which time fine powders were removed and stored.

#### 2.2. Methods

The thermal properties of the milled polymers were



Fig. 1. Gel permeation chromatograms of h-PMMA cryomilled for different times ( $t_m$ , shown in the figure) indicating that the PMMA molecular weight decreases with increasing  $t_m$ . Note that the distribution initially broadens but eventually narrows, indicating preferential scission of long chains. The chromatograms displayed here are shifted vertically to facilitate comparison.

characterized by differential scanning calorimetry (DSC) with a DuPont Instruments 910 calorimeter, operated at a heating rate of 20°C min<sup>-1</sup> under an Ar purge. Molecular weight measurements were performed as a function of milling time ( $t_m$ ) by GPC with a Waters 2690 injection unit and Styragel<sup>®</sup> HR4 columns. Light scattering and differential pressure measurements were concurrently performed at ambient temperature from 10 mg ml<sup>-1</sup> polymer solutions in THF (100 µl injections at a flow rate of 1 ml min<sup>-1</sup>) with a Wyatt Technology Interferometric

Refractometer and a Viscotek T60A dual detector, respectively. Sol–gel analysis was conducted by vacuum-assisted filtration on cryomilled PI (0.4 wt% in toluene) using Fisher quantitative filter paper Q2 (particle retention <1  $\mu$ m). Fourier-transform infrared (FTIR) spectroscopy was performed on cryomilled PI from 400 to 4000 cm<sup>-1</sup> (at a resolution of 2 cm<sup>-1</sup>) with a Nicolet Magna-IR Spectrometer 750 equipped with an attenuated total reflectance (ATR) cell and a ZnSe crystal. All non-calorimetric measurements were performed at ambient temperatures.

The impact strength of milled PMMA specimens was measured at 25°C on a Tinius-Olsen 92T impact tester modified to accept short (10 mm) samples. Impact samples were prepared by compacting ca. 1.6 g of powder to a disk 25 mm in diameter at ambient temperature and 88 MPa for 5 min. These disks were next melt-pressed into squares with minimal pressure at a temperature 40°C above the measured  $T_{g}$  of the powder (ranging from 100 to 160°C, depending on  $t_{\rm m}$ ) for 5 min, then quenched to ambient temperature in water. The squares were 2 mm thick and 25.4 mm on a side, and were subsequently cut into "matchsticks" measuring 2 mm  $\times$  4 mm  $\times$  25 mm with a Buehler Isomat diamond saw. Each matchstick was placed 5 mm into the clamp of the impact tester and oriented such that the striker hit the 2 mm side and fracture occurred along the 4 mm side. The matchsticks were not notched. A torque of 60 N-cm was applied to the clamp, which exerted a force of 330 N. After initial fracture, the remaining part of the matchstick



Fig. 2. Dependence of  $\overline{M}_n$  (open symbols) and  $\overline{M}_w$  (filled symbols) on  $t_m$  for: (a) h-PMMA subjected to cryomilling (circles, solid lines) and ambimilling (triangles, dashed lines); (b) cryomilled m-PMMA; (c) cryomilled l-PMMA; and (d) cryomilled PEP. The lines correspond to regressed fits of Eq. (1) in the text, and resulting parameters are included in Table 3.

$t_{\rm m}$ (h)	h-PMMA (cryomilled)	h-PMMA (ambimilled)	m-PMMA	l-PMMA	n-PMMA	PEP
0.0	4.08	4.08	1.80	1.12	1.25	1.06
1.0	5.61	3.81	2.23	1.11	1.78	1.10
2.0	5.83	4.11	2.22	1.10	2.16	1.26
3.5	5.21	2.60	2.12	1.11	1.56	1.41
5.0	4.21	1.45	1.65	1.08	1.35	1.25
7.5	12.87	1.14	1.86	1.08	_	1.69
10	21.82	1.05	1.22	1.10	-	1.52

Table 2 Measured polydispersity indices of PMMA and PEP as a function of milling time

was subjected to impact testing twice more until it became too short for testing. About 15 measurements were acquired from each specimen, and as many as two outlying measurements were discarded per specimen.

#### 3. Results and discussion

## 3.1. Molecular weight

To ascertain the effect of high-energy mechanical milling on the molecular weight distribution of each homopolymer examined here, GPC was performed on solutions of the asmilled materials in THF. Fig. 1 shows a set of concentration curves obtained for h-PMMA cryomilled for different  $t_m$  up to 10 h. The data presented in Fig. 1 represent the output signal from the refractometer and are scaled and offset to facilitate comparison. According to the data tabulated in Table 1, the h-PMMA polymer possesses a relatively high target molecular weight and polydispersity index (PDI =  $\overline{M}_{\rm w}/\overline{M}_{\rm n}$ ). Upon mechanical milling, the peak in the chromatogram from the as-received material initially becomes less intense, and then broadens and shifts to longer retention times with increasing  $t_{\rm m}$ . Eventually, however, the peak begins to intensify and, once again, becomes relatively narrow at long  $t_{\rm m}$ . These results reveal two important trends: (i) the molecular weight of h-PMMA decreases with increasing  $t_{\rm m}$ ; and (ii) the molecular weight distribution initially broadens before narrowing as low-molecularweight chains are produced during milling.

Calculated values of  $\overline{M}_n$  and  $\overline{M}_w$  derived from GPC traces such as those provided in Fig. 1 are displayed as a function of  $t_m$  in Fig. 2 for h-PMMA (Fig. 2a), m-PMMA (Fig. 2b), l-PMMA (Fig. 2c) and PEP (Fig. 2d). In all cases, both average molecular weights are observed to decrease substantially with increasing  $t_m$ , with the magnitude of reduction varying from a factor of 2 (PEP) to a factor of 130 (ambimilled h-PMMA). Results obtained for both cryomilled and ambimilled h-PMMA are included for comparison in Fig. 2a and reveal that ambimilling yields a much more pronounced reduction in molecular weight than cryomilling. Corresponding PDI values, provided in Table 2, initially increase with increasing  $t_m$  in both series, but remain large (PDI > 4.08) for cryomilled h-PMMA. In

marked contrast, ambimilling eventually yields a nearly monodisperse molecular weight distribution (PDI = 1.05) at the cost of an extremely depressed molecular weight  $(\bar{M}_{\rm w} = 7.99 \text{ kg mol}^{-1})$ , in h-PMMA. Comparable behavior is observed for cryomilled m-PMMA (Fig. 2b), viz. the PDI initially increases before decreasing with increasing  $t_{\rm m}$ , without such a dramatic decline in molecular weight. For cryomilled 1-PMMA (Fig. 2c), both  $\overline{M}_n$  and  $\overline{M}_w$  are seen to decrease at similar rates with respect to  $t_{\rm m}$  (a factor of about three reduction in each is achieved after 10 h of cryomilling), indicating that the polydispersity in this material remains nearly constant with  $t_{\rm m}$ . It is of interest to note that the  $\overline{M}_n$  and  $\overline{M}_w$  values obtained from h-PMMA and m-PMMA cease decaying at values higher than the initial values of m-PMMA and 1-PMMA, respectively. This indicates that the milled PMMA possesses intrinsically different behavior relative to the unmilled polymer when subjected to extended milling.

The cryomilling-induced changes in molecular weight recorded for PEP are presented in Fig. 2d and clearly do not follow the trends described above for PMMA. For this homopolymer, the molecular weight decreases by a factor of 2-3 at  $t_{\rm m} = 10$  h, but the polydispersity continues to increase monotonically with increasing  $t_{\rm m}$  (see Table 2). Since the rate of molecular weight reduction appears to be significantly slower for PEP than for PMMA, it is possible that, on one hand, PDI convergence may simply not have been attained during the course of  $t_{\rm m}$  examined. On the other hand, this disparity in the milling-induced evolution of molecular weight distribution may reflect a fundamental difference between the physico-chemical responses of PEP and PMMA to solid-state milling. Additional analysis in this vein with the PI homopolymer is, unfortunately, not possible due to the insolubility of cryomilled PI, which precludes GPC analysis. This observation is discussed further later in this work.

One approach by which the molecular weight trends evident in Fig. 2 can be analyzed has been suggested by Baramboim [21], who explored the molecular weight degradation of polymers subjected to mechanical processing. In this analysis, the time-dependent molecular weight of a polymer is given by

$$M(t_{\rm m}) = M_{\infty} + a \,\mathrm{e}^{-kt_{\rm m}} \tag{1}$$



Fig. 3. Variation of (a)  $\overline{M}_n$  ( $\bigcirc$ ) and  $\overline{M}_w$  ( $\bullet$ ) and (b) the PDI with  $t_m$  for n-PMMA, which possesses an initially narrow molecular weight distribution (PDI = 1.24). Note that the PDI initially increases and subsequently decreases with increasing  $t_m$ .

where  $M_{\infty}$  denotes the molecular weight of the polymer that cannot be reduced further, *a* is a constant and *k* represents a degradation constant, which is sensitive to the milling parameters, as well as to polymer chemistry and chain conformation. Provided in Table 3 are values of  $M_{\infty}$  and *k* discerned from a non-linear least-squares fit of Eq. (1) to the  $\bar{M}_n$  data in Fig. 2. To place these values in perspective, Baramboim [21] reports  $M_{\infty} = 9.0$  kg mol<sup>-1</sup> and k =0.12 h<sup>-1</sup> for PMMA subjected to a mechanical process that is not explicitly detailed. Thus, the values deduced for *k* in this work are generally (and markedly) higher than those reported elsewhere, indicating that mechanical milling is a much higher energy technique than the one employed by Baramboim [21].

Examination of the data in Table 3 yields several important conclusions. First, the values of  $M_{\infty}$  and k differ depending on initial PMMA molecular weight and milling temperature (ambimilled versus cryomilled). Both  $M_{\infty}$  and k appear to increase non-linearly with increasing  $\bar{M}_n$  (or, alternatively,  $\overline{M}_{\rm w}$ ) of the unmilled PMMA. Similar variation of  $M_{\infty}$  with initial polymer molecular weight has been previously observed [22] in mechanically processed systems. Furthermore, values of  $M_{\infty}$  and k for the h-PMMA and m-PMMA homopolymers are comparable in magnitude. Such similarity may not be surprising since both h-PMMA and m-PMMA possess initial  $\overline{M}_n$  values far in excess of the critical molecular weight of entanglement ( $M_c = 27.5 \text{ kg mol}^{-1}$ ) for PMMA [26,27]. In the present study, it is interesting to note that, in the PMMA homopolymers initially with  $\bar{M}_{\rm n} > M_{\rm c}, M_{\infty}$  only differs from  $M_{\rm c}$  by as much as about 15% (for h-PMMA), suggesting that cryomilling may not shorten long, entangled PMMA molecules below the limit of molecular entanglement.

Here, we return to the observation made earlier concerning the initial broadening and subsequent narrowing of the PMMA molecular weight distribution. This trend can be attributed to the high probability of preferentially breaking long molecules at short  $t_m$  and the generally lower probability associated with breaking short chains [21,22]. While the molecular weight and PDI data presented so far are consistent with this explanation, the PDI values of the initial (unmilled) h-PMMA and m-PMMA homopolymers are excessively high (4.08 and 1.80, respectively) to confirm this conclusion. This explanation can be tested more rigorously through the use of the PMMA homopolymer with  $\bar{M}_{\rm n} > M_{\rm c}$  and a relatively low PDI (designated in Table 1 as n-PMMA). The time evolution of molecular weight and polydispersity in this homopolymer is shown in Fig. 3 for ambimilling times up to 5 h. Inspection of this figure reveals similar trends as those previously observed for the initially polydisperse PMMA homopolymers: (i) a sharp reduction in molecular weight by approximately an order of magnitude at short  $t_m$ ; and (ii) an initial increase in PDI, followed by a comparable decrease (with a maximum PDI observed in the vicinity of  $t_{\rm m} = 2$  h). Fig. 3 therefore confirms the preferential breaking of long PMMA chains during the collisions that occur in high-energy mechanical milling at ambient or cryogenic temperatures.

Another trend evident from the data listed in Table 3 is that ambimilling PMMA yields a lower  $M_{\infty}$ , but higher k (by almost a factor of two), than cryomilling, indicating that

Table 3 Regressed parameters derived for several polymers upon mechanical milling

Sample designation (process)	$M_{\infty}$ (kg mol <sup>-1</sup> )	$k (h^{-1})$	$T_{\rm g}^{\infty}$ (°C)	$\alpha \times 10^{-5} (\text{kg }^{\circ}\text{C mol}^{-1})$
h-PMMA (cryomilled)	27	0.93	123.2	8.54
h-PMMA (ambimilled)	13	1.83	122.4	7.07
m-PMMA (cryomilled)	23	0.86	123.0	13.0
1-PMMA (cryomilled)	5.1	0.41	-	_
n-PMMA (ambimilled)	9.6	1.14	-	-
PEP (cryomilled)	20	0.54	_	-



Fig. 4. Differential scanning calorimetry thermograms of h-PMMA subjected to cryomilling for different milling times ( $t_m$ , shown in the figure). These are all second-heat traces acquired at 20°C min<sup>-1</sup> under Ar (first-heat data include distracting stress-related thermal responses).

ambimilling causes more molecular degradation than cryomilling. This result may be somewhat counterintuitive, since polymer chains are anticipated to become increasingly embrittled with decreasing temperature. Previous studies have, however, reported that mechanical degradation increases substantially with decreasing temperature above  $T_{\rm g}$ , but increases with increasing temperature below  $T_{\rm g}$ [21,28]. In both ambimilling and cryomilling, the vial temperatures are well below the  $T_{\rm g}$  of PMMA. The internal temperature rise, instantaneously fluctuating due to the high-energy collisions of the ball bearings, is not known with any degree of precision. Theoretical and experimental estimates of the local temperature increase (derived from milling-induced structural changes in inorganic materials) suggest that the increase can range from 10 to 400°C, depending primarily on mill type. For the SPEX mill employed here, however, an increase of less than 50°C is expected [17]. Since molecular weight degradation is more pronounced in the ambimilled PMMA relative to its cryomilled analog, PMMA most likely remains in its glassy state during both ambimilling and cryomilling. If, however, the local temperature increase became sufficiently high to heat



Fig. 5. Glass transition temperature shift,  $\Delta T_g = T_g(t_m) - T_{g,0}$ , presented as a function of  $t_m$  for cryomilled h-PMMA ( $\bigcirc$ ), ambimilled h-PMMA ( $\bigcirc$ ), m-PMMA ( $\triangle$ ) and l-PMMA ( $\diamond$ ). The lines (solid for cryomilled samples and dashed for ambimilled samples) serve as guides for the eye.



Fig. 6. Dependence of  $\Delta T_g$  on  $t_m$  for cryomilled PEP ( $\bigcirc$ ) and PI ( $\triangle$ ). While PEP exhibits the same response as PMMA to increasing  $t_m$  (see Fig. 5), the change in  $\Delta T_g$  for PEP occurs more slowly. Note that the time-dependent behavior of PI differs markedly from PMMA and PEP. The error bars denote one standard deviation in the data and provide a measure of reproducibility.

the polymer above its  $T_{g}$ , the rate of chain damage at a given  $t_{m}$  due to ambimilling would be less than that due to cryomilling (assuming negligible thermo-oxidative effects) [21,28].

The explanation for enhanced molecular weight reduction due to ambimilling relative to cryomilling lies in the thermodynamics of chain scission. In the case of mechanical degradation in the solid state, the activation energy required to break molecular bonds is supplied by an external stress applied to a polymer chain. The normal thermal vibrations of the atoms comprising the chain augment this stress. For a given stress state, it is therefore possible for a bond to be stable at one temperature, but unstable at a higher temperature [24]. Since the temperature difference between ambimilling and cryomilling in the present study is approximately 200°C, a much higher stress is required for chain scission during cryomilling relative to ambimilling. From the results obtained here, it can be concluded that mechanical milling of PMMA becomes increasingly more efficient with increasing temperature insofar as the PMMA remains in the solid (glassy) state. Comparable behavior has also been observed in the mechanical milling of PET [25] and polystyrene (data not shown), and may constitute a general response of thermoplastics to high-energy milling.

#### 3.2. Glass transition temperature

According to the data presented in the previous section, mechanical milling has a significant impact on the molecular weight of PMMA and PEP. It is therefore reasonable to expect that M-dependent properties of these materials will likewise be affected. A thermal property that is sensitive to molecular weight is  $T_g$ , which for nearly monomolecular linear polymers can be conveniently written as [29,30]

$$T_{\rm g} = T_{\rm g}^{\infty} - \alpha \bar{M}_{\rm n}^{-1} \tag{2}$$

Here,  $T_g^{\infty}$  denotes the  $T_g$  in the limit as  $\bar{M}_n \rightarrow \infty$  (which is valid in the mean-field limit) and  $\alpha$  is a polymer-specific



Fig. 7. Glass transition temperature presented as a function of  $\overline{M}_n^{-1}$  for (a) cryomilled h-PMMA, (b) ambimilled h-PMMA; and (c) m-PMMA. A linear least-squares fit of Eq. (1) in the text (solid line) to each data set at short  $t_m$  yields the values of  $T_g^{\circ}$  and  $\alpha$  listed in Table 3. The data are more accurately represented through the use of Eq. (3) in the text (dashed line).

constant. To ascertain the effect of high-energy mechanical milling on  $T_g$ , DSC thermograms have been acquired from all of the as-milled polymers and are displayed for cryo-milled h-PMMA in Fig. 4. Note that these thermograms correspond to second heating scans, since the first scans (not shown here) exhibit distracting stress-related features (the focus of this section is on the milling-induced M-dependence of  $T_g$ ). Examination of the thermograms in Fig. 4, which are illustrative of the m-PMMA and l-PMMA homopolymers, reveals that the  $T_g$  of the h-PMMA sample decreases, and that the  $T_g$  transition broadens markedly, with increasing  $t_m$ .

Analysis of thermograms such as those in Fig. 4 to extract midpoint  $T_{gs}$  yields the results presented in Fig. 5. In this

figure,  $\Delta T_{g}$ , defined as  $T_{g}(t_{m}) - T_{g,0}$  where  $T_{g,0}$  denotes the  $T_{\rm g}$  of the unmilled polymer, is provided as a function of  $t_{\rm m}$ for both cryomilled and ambimilled h-PMMA,  $(T_{g,0} =$ 125°C), cryomilled m-PMMA ( $T_{g,0} = 112$ °C) and cryomilled 1-PMMA ( $T_{g,0} = 94^{\circ}$ C). In all cases, a decrease in  $T_{g}$  (by as much as ca. 50°C) is observed as  $t_{m}$  is increased. This figure also shows that the milling-induced decrease in PMMA  $T_g$  is not a simple function of molecular weight in the cryomilled PMMA series, since the maximum  $T_{g}$  reduction beyond  $t_m = 5 h$  occurs in order (from highest to lowest) in m-PMMA, h-PMMA and l-PMMA. A possible explanation for this order is that the h-PMMA homopolymer possesses a very high PDI (4.08), whereas those of m-PMMA and 1-PMMA are less than 2.00. In addition, the milling temperature is seen to have a substantial impact on  $T_{\rm g}$ , with ambimilling promoting a much larger drop in the  $T_{g}$  of h-PMMA than cryomilling (ca. 50°C versus 30°C, respectively). This observation is consistent with the more pronounced effect of ambimilling on h-PMMA molecular weight degradation. It should be recognized that, if the reduction in  $T_{\rm g}$  is sufficient, local heating generated during ambimilling may cause the h-PMMA to behave as a melt. Recall that the susceptibility of molten polymer chains to break during high-energy ball milling differs markedly from that of chains frozen in the solid state [21,28].

Fig. 6 shows the time-dependent variation of  $\Delta T_{\rm g}$  for PI and PEP, for which the values of  $T_{g,0}$  are equal to -55.5 and  $-51.7^{\circ}$ C, respectively. The cryomilled PEP is seen to emulate the same behavior recorded for the PMMA samples in Fig. 5, although it is unclear from the data in Fig. 6 whether a limiting value of  $\Delta T_{\rm g}$  has been reached after  $t_{\rm m} =$ 10 h. An interesting difference between the data for PMMA and PEP in Figs. 5 and 6, respectively, is that the magnitude of  $\Delta T_{g}$  is consistently smaller for PEP. In marked contrast, cryomilled PI does not even exhibit an initially monotonic reduction in  $\Delta T_g$ . Instead,  $\Delta T_g(t_m)$  attains a sharp minimum at a relatively short  $t_{\rm m}$  (2 h) and subsequently increases almost back to zero, decreasing slightly from zero (by about 2.7°C at  $t_{\rm m} = 10$  h) thereafter. This behavior, which is completely reproducible (as evidenced by the error bars included in Fig. 6) is indicative that cryomilling affects PI differently relative to PMMA and PEP. Recall from the previous section that the molecular weight distribution of PI could not be measured by GPC due to insolubility of cryomilled PI in the carrier solvent. The sharp increase in the  $T_{\rm g}$  (or, alternatively,  $\Delta T_{\rm g}$  in Fig. 6) of cryomilled PI after  $t_{\rm m} = 2$  h, accompanied by its apparent insolubility, strongly suggests that the PI chains undergo chemical crosslinking during cryomilling. In this case, we envisage a highly dynamic competition between chains breaking (causing a decrease in molecular weight) and crosslinking (promoting an increase in molecular weight) under highly non-equilibrium conditions. We return to this topic in the final section of this study.

As indicated by Eq. (2),  $T_g$  can depend sensitively on  $\bar{M}_n$ when  $\bar{M}_n$  becomes relatively small, as is the case here. The



Fig. 8. Variation of impact strength with  $t_m$  for cryomilled h-PMMA ( $\bigcirc$ ), ambimilled h-PMMA ( $\bigcirc$ ) and cryomilled m-PMMA ( $\triangle$ ). The lines shown in this figure (solid for cryomilled samples and dashed for ambimilled samples) serve as guides for the eye. Error bars denote one standard deviation in the data.

dependence of  $T_{\rm g}$  on  $\bar{M}_{\rm n}$  for milled h-PMMA and m-PMMA (I-PMMA is not included here due to the slight variation of  $T_{\rm g}$  with  $t_{\rm m}$ , <10°C, in Fig. 5) is evident in Fig. 7, in which  $T_{\rm g}$ is presented as a function of  $\bar{M}_n^{-1}$  for cryomilled h-PMMA (Fig. 7a), ambimilled h-PMMA (Fig. 7b) and cryomilled m-PMMA (Fig. 7c). According to each of these figures a simple linear relationship between  $T_{\rm g}$  and  $\bar{M}_{\rm n}^{-1}$  does not accurately represent the data shown. Application of Eq. (2) to each of the data sets in Fig. 7 at short  $t_{\rm m}$ , however, yields reasonable regressed fits from which values of  $T_g^{\infty}$ and  $\alpha$  can be extracted. These constants are provided for comparison in Table 3 and, despite the highly nonequilibrium manner in which the homopolymers have been processed (in marked contrast to the highly controlled fractionation methods [29] used to obtain nearly monodisperse homopolymers of known  $\overline{M}_n$ ), are in fair agreement with the values of  $T_g^{\infty}$  and  $\alpha$  reported [31,32] elsewhere: 114–125°C for  $T_g^{\infty}$  and  $(0.94-3.4) \times 10^5$  for  $\alpha$ .



Fig. 9. Impact strength as a function of  $\overline{M}_n$  on double-logarithmic coordinates illustrating the dependence of impact strength on  $\overline{M}_n$  for cryomilled h-PMMA ( $\bigcirc$ ), ambimilled h-PMMA ( $\bigcirc$ ) and cryomilled m-PMMA ( $\triangle$ ). At high  $\overline{M}_n$ , the impact strength is nearly independent of  $\overline{M}_n$  (dashed line). At lower  $\overline{M}_n$ , impact strength varies almost linearly with  $\overline{M}_n$  (solid line). At  $\overline{M}_n$  below  $M_0$  (the range of  $M_0$  is shown by the shaded area), the impact strength decreases abruptly (dotted line) due to insufficient molecular entanglement. Error bars denote one standard deviation in the data.

Such agreement regarding  $T_g^{\infty}$  is surprising, especially because high-energy mechanical milling initially tends to produce very broad molecular weight distributions (see Table 2), which can have a tremendous effect on the measured value of  $T_{g}$  [32]. The consistently higher values of  $\alpha$  obtained here indicate that the  $T_{g}$  of milled PMMA is more sensitive to  $\overline{M}_n$  than monodisperse PMMA fractions. While the data in Fig. 7 have been examined by established means (Eq. (2)) to glean insight into the relationship between  $T_{\rm g}$  and  $\bar{M}_{\rm n}$  in mechanically milled PMMA, such analysis is plainly incapable of fully describing this relationship. Examination of Fig. 7 reveals that, at long  $t_m$  and, hence, low  $\bar{M}_{n}$ ,  $T_{g}$  appears to reach a limiting value, suggesting that the  $T_g$  in these milled PMMA grades is better represented by an expression similar to Eq. (1) than by Eq. (2). Regression of an exponential function of the form

$$T_{\rm g}(M) = T_{\rm g}^* + b {\rm e}^{-k^* M}$$
 (3)

to each of the data sets in Fig. 7 accurately reflects the experimental data in each case, although the precise physical meaning of the regressed parameters  $T_g^*$  and k' obtained upon doing so is not clear. It is interesting to note that the values of k' derived for cryomilled h-PMMA (Fig. 7a) and m-PMMA (Fig. 7c) are comparable in magnitude: 0.89 and 0.94 mol kg<sup>-1</sup>, respectively. Recall that similar agreement exists for the molecular-weight degradation constant (k) in Table 3.

One final factor that has been ignored in the present analysis is the dependence of  $T_g$  on PMMA tacticity. Tacticity alone can be responsible for differences of ca. 75°C in the reported [32] value of  $T_g^{\infty}$ . No effort has, however, been made here to discern the initial tacticity of the PMMA grades used in the present study. Milling-induced chemical modification of macromolecules certainly constitutes an important topic for future investigation in the present vein.

### 3.3. Impact strength

To establish the effect of mechanical milling on the physical properties of PMMA, impact testing has been performed on specimens before and after milling. Results of these tests are displayed in Fig. 8 for h-PMMA (cryomilled and ambimilled) and m-PMMA (data for the 1-PMMA grade could not be obtained due to insufficient sample cohesion upon melt pressing). Both as-received PMMA grades possess an impact strength of about 11 J m<sup>-1</sup>, which compares favorably with values reported elsewhere [30,33] for PMMA, typically  $10-16 \text{ Jm}^{-1}$ . As anticipated from the degradation in  $\overline{M}_{n}$  observed in earlier sections, mechanical milling induces a dramatic reduction in impact strength. According to the data in Fig. 8, the impact strength of cryomilled h-PMMA is the least affected by milling when  $t_{\rm m} < 8$  h. The impact strength decreases to about 4 J m<sup>-1</sup> after 3.5 h of cryomilling and falls below  $2 \text{ Jm}^{-1}$  after 10 h of milling. More pronounced reductions in impact strength (to below  $1 \text{ Jm}^{-1}$  after 5 h of milling) are realized in both the



Fig. 10. Results from the sol-gel analysis of cryomilled PI. In (a), the soluble PI fraction (*S*) is shown as a function of  $t_m$ , with the solid line provided as a linear least-squares fit to the data. In (b), a Charlesby–Pinner plot showing the dependence of  $S + S^{1/2}$  on  $t_m^{-1}$  for long  $t_m$  is displayed. A linear fit of these data to Eq. (4) yields the fracture and crosslinking densities per unit  $t_m$ . These parameters can be used to determine the crosslinking coefficient ( $\delta$ ), included as a function of  $t_m$  (solid line) in (c). The dashed line in (c) represents the value of  $\delta$  in the limit as  $t_m \rightarrow \infty$ .

ambimilled h-PMMA and cryomilled m-PMMA specimens. Such discouraging performance is consistent with the fact that PMMA is a very brittle thermoplastic and is highly susceptible to mechanical damage [21,34].

The reduction in impact strength of mechanically milled PMMA is attributed to the accompanying decrease in molecular weight, since prior studies [27,35–39] have demonstrated that the strength and impact resistance of thermoplastics depend sensitively on molecular weight. Fig. 9 shows the variation of impact strength with  $\bar{M}_n$  for all of the milled specimens included in Fig. 8 and confirms that the impact strength of milled PMMA depends on  $\bar{M}_n$ . Previous efforts have identified three distinct regions describing the molecular weight dependence of impact strength. At high molecular weights ( $\bar{M}_n > 150 \text{ kg mol}^{-1}$ for PMMA [27]), impact strength is virtually independent on  $\bar{M}_n$ . Below this threshold, impact strength has been found to vary almost linearly with  $\bar{M}_n$ . The third detected regime occurs at  $\bar{M}_n < M_0$ , where  $M_0$  is marginally less than  $M_c$ ( $M_0$  has been measured [27,36,39] between 20 and 23 kg mol<sup>-1</sup>). Within this regime, little if any impact strength can be measured due to insufficient molecular entanglement. While the impact strength data collected here exhibit experimental scatter, at least some of these features are present in Fig. 9.

As illustrated by the dashed horizontal line in Fig. 9, impact strength does not appear to be strongly dependent on  $\bar{M}_n$  at high  $\bar{M}_n$ . At lower  $\bar{M}_n$ , impact strength is accurately described by a linear dependence on  $\overline{M}_n$  (shown by the solid line in Fig. 9). The intersection between the horizontal line at high  $\bar{M}_n$  and the regressed linear fit at intermediate  $\overline{M}_n$  occurs at about 135 kg mol<sup>-1</sup> (which is in reasonably good agreement with 150 kg mol<sup>-1</sup> from Ref. [27]). Below the  $M_0$  range, impact strength no longer decreases linearly with  $\bar{M}_n$  but instead scales as  $\bar{M}_n^{1.7}$ (dashed line in Fig. 9). In this case, the intersection between the linear fit at intermediate  $\bar{M}_n$  and the power-law fit at low  $\bar{M}_n$  ( $\leq M_0$ ) occurs at about 21 kg mol<sup>-1</sup>, which corresponds, within reported values, to  $M_0$  of PMMA. Thus, the data in Fig. 9 dictate that  $\overline{M}_n$  of mechanically milled PMMA cannot drop below  $M_0$  if reasonable fracture resistance is desired. These data likewise provide a measure by which the upper limit on  $t_m$  (7.5 h for cryomilled h-PMMA and 10 h for m-PMMA) can be ascertained.

## 3.4. Chemical interactions

A sol-gel analysis has been performed to quantitate the fraction of milling-induced insoluble PI. The soluble fraction (*S*) of PI discerned from this analysis is presented as a function of  $t_m$  in Fig. 10. This graph verifies that the asreceived PI is completely soluble in toluene, since no polymer is retained in the filter paper. After cryomilling for just for 1 h, however, a nontrivial fraction of insoluble PI is retained, increasing with an increase in  $t_m$ . This trend clearly indicates that PI undergoes interchain crosslinking during high-energy mechanical milling, and likewise explains the measured increase in the  $T_g$  of milled PI: crosslinking decreases the free volume of neighboring chains and increases the observed  $T_g$ .

The molecular evolution of PI during cryomilling can be more clearly elucidated in terms of a Charlesby–Pinner analysis. This treatment, originally developed as a means to explore the effect of radiation on polymers, relates exposure dose to radiation-induced molecular changes in polymers, such as crosslinking [40–43]. It relies on the presumption that crosslinking and chain scission occur



Fig. 11. FTIR spectra of cryomilled PI at  $t_m$  of 0 h (thin line) and 10 h (thick line). Full spectra are shown in (a), whereas (b) and (c) display enlargements of intervals in which differences between the two samples are evident. Peak assignments are discussed in the text.

simultaneously at random throughout the polymer, a condition that is believed to be sufficiently satisfied during highenergy mechanical milling. The relationship between *S* and dose (*r*) for a polymer possessing a random initial molecular weight distribution (PDI = 2.0) is given by [41]

$$S + S^{1/2} = \frac{2}{\delta} = \frac{p}{q} + \frac{1}{qNr}$$
(4)

where  $\delta$  is the number of crosslinks per initial weight-average molecule, q represents the crosslink density per unit radiation dose, p is the fracture density per unit radiation dose and N denotes the number-average degree of polymerization. For other, non-random molecular weight distributions, Eq. (4) may be employed if r, and the number of chain scission events, is sufficiently high, in which case the molecular weight distribution can be considered nearly random.

To deduce the crosslinking coefficient ( $\delta$ ) promoted by mechanical milling, r in Eq. (4) is replaced by its mechanical analog  $(t_m)$ . Shown in Fig. 10b is the dependence of  $(S + S^{1/2})$  on  $t_m^{-1}$  at "long"  $t_m$  (2–10 h). A linear leastsquares fit of the data in Fig. 10b yields p/q = 0.64 and 1/qN = 2.00. Incorporating these values into Eq. (4) results in the time-dependent  $\delta$  provided in Fig. 10c. Note that the value of  $\delta$  at infinite  $t_m$  is also identified in this figure. Calculation of N (= 1012 from GPC analysis) reveals that q and p are equal to  $4.9 \times 10^{-4}$  and  $3.2 \times 10^{-4}$ , respectively. These values, which are dependent on milling conditions, indicate that chemical crosslinking is more likely (by about 50%) than scission during PI cryomilling. Determination of these Charlesby-Pinner parameters permits quantitation of the effects of high-energy mechanical milling on a crosslinkable polymer such as PI.

If sufficiently numerous, specific chemical changes in the cryomilled polymers examined here can be identified by FTIR spectroscopy. While no discernible changes are observed in the milled PMMA and PEP specimens, unmistakable FTIR spectral changes are detected in the milled PI samples. The FTIR spectra presented in Fig. 11a, offset to facilitate comparison correspond to PI in the as-received state ( $t_{\rm m} = 0$  h) and after cryomilling for 10 h. The principal features in the spectra identically match those reported in previous works, and the peak assignments are provided elsewhere [44]. Close examination of these spectra reveals milling-induced differences in the vicinity of 700 and 1750 cm<sup>-1</sup>. Enlargements of these regions (without signal offset) are shown in Fig. 11b and c and confirm the existence of three small peaks (at 1745, 729 and 694  $\text{cm}^{-1}$ ) that are present in the cryomilled sample but not in the virgin PI. To properly assign these new absorbance peaks, we first examine the chain fracture process and subsequent reaction pathways of radicals produced in previous studies [45,46] of PI degradation.

The CH2-CH2 bond has been found to be the weakest bond in PI and is prone to rupture under mechanical stress. Chain scission at this bond is depicted in Scheme 1, in which a PI chain (a) is divided to form the radicals (b) and (c). These radicals may undergo resonance stabilization to form (d) and (e) and subsequently react, depending on milling conditions. In the absence of oxygen, three reaction pathways have been identified. The first of these involves the recombination of radicals (b) and (c) to reform a virgin PI chain. Another possibility is that the radicals react with an unsaturated bond of another molecule and form a crosslink (f), which can lead to the formation of a permanent network or gel. The last possibility is that an original radical (c) recombines with a resonance-stabilized radical (d) to form a PI chain with a pendant vinyl group (g). This reaction, only observed in high-purity Ar, is effectively prevented [45] in the presence of either N<sub>2</sub> or O<sub>2</sub>. In the presence of oxygen, PI radicals react rapidly with O2 molecules to produce peroxy



Scheme 1.

radicals (**h**), which may subsequently extract hydrogen from other molecules. If hydrogen is extracted from other PI molecules, further crosslinking will ensue.

On the basis of these possible reaction pathways, as well as prior FTIR assignments [47,48], the absorbance peaks produced during the cryomilling of PI (see Fig. 11b and c) are assigned the following vibration modes. The peak located at 694 cm<sup>-1</sup> is attributed to the CH wag in the pendant vinyl group. The peak at 729 cm<sup>-1</sup> may be associated with activation of the cis-CH wag of R-CH=CH-R groups due to nearby chain scission that occurs during milling, or the CH<sub>2</sub> rock of the molecules activated by the formation of either (i) (CH<sub>2</sub>)<sub>3</sub>-CH<sub>3</sub> groups via chain decomposition [47] or (ii) PI crystals [48] due to mechanical milling. (Such induced crystallization has been previously observed [45] during the mastication of natural rubber.) The excitation observed at 1745 cm<sup>-1</sup> is sufficiently broad to accommodate several different molecular excitations that all involve oxygen [47,49-52]. Since milling is conducted in the absence of  $O_2$ , the presence of  $O_2$  in the cryomilled PI FTIR spectrum strongly suggests the residual free radicals produced during milling react with atmospheric  $O_2$  upon sample removal from the milling vial.

One final observation warranting discussion at this juncture is that the chemical crosslinking of PI, as well as the rapid molecular-weight reduction of PMMA and slower deterioration of PEP, during high-energy ball milling are remarkably consistent with the response of these materials to high-energy radiation [43,53]. Moreover, PET has been found [25,54] to be chemically resistant to mechanical milling and radiation exposure, both of which promote solid-state amorphization in metallic alloys [55,56]. A general correlation between the high-energy mechanical milling and irradiation of polymeric materials would permit use of the established body of work on polymer radiation damage to predict suitable polymer candidates that would be most resistant to milling-induced molecular modification.

### 4. Conclusions

In this study, three different polymers—PMMA, PI and PEP—have been subjected to high-energy mechanical milling to investigate their response to this solid-state processing technique. Results obtained here clearly demonstrate that mechanical milling of PMMA yields a substantial reduction in molecular weight, with larger chains breaking preferentially. In the case of polymers with an initial molecular weight above the critical molecular weight of entanglement, a lower molecular-weight limit (near the entanglement molecular weight) is identified below which chain scission proceeds very slowly. This behavior is consistent with the degradation of PMMA under mechanical strain [21,22], but occurs at a much higher rate due to the more vigorous action of milling. Accompanying the milling-induced decrease in molecular weight are reductions in both the glass transition temperature and impact strength of PMMA. The dependence of impact strength on molecular weight varies with molecular weight regime, with the impact strength becoming negligibly small as the molecular weight is reduced below the chain entanglement limit. The value of this limiting molecular weight is estimated from the results acquired here to be about 21 kg mol<sup>-1</sup>. Moreover, milling performed at ambient temperature more severely degrades the molecular weight of PMMA than milling conducted at cryogenic temperatures. This observation is attributed to the increase in atomic thermal vibrations, which augment chain scission, by mechanical strain.

For the PI and PEP, the effects of cryogenic mechanical milling depend strongly on polymer type. Mechanical milling of saturated PEP results in monotonic reductions in molecular weight and glass transition temperature. Relative to PMMA, however, the rate of molecular weight degradation is much slower, and a narrowed molecular weight distribution is not observed. The unsaturated PI exhibits a substantially different response to mechanical milling than does PEP. Crosslinking of PI chains yields an insoluble fraction that increases with increasing milling time. Corresponding glass transition temperature measurements show a large initial decrease, followed by almost complete recovery due to chemical crosslinking. Crosslinking analysis based on the Charlesby-Pinner treatment developed for radiationinduced scission/crosslinking indicates that: (i) 2.4 crosslinks per initial weight-average molecule form after 10 h of milling; and (ii) crosslinking is  $1.5 \times$  more likely than chain scission for PI during mechanical milling. Spectroscopy of milled PI reveals three milling-induced peaks, which confirm the formation of new chemical bonds during milling. These results demonstrate that the effect of highenergy mechanical milling on polymers can be profound. While solid-state mechanical milling holds the promise of yielding nanoscale-mixed polymer blends from two or more chemically dissimilar macromolecules [57-59], millinginduced changes in molecular structure and chemistry, such as those identified here, must be considered carefully if this strategy is to be explored as a viable processing technology.

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